Math 222 Rahman

Remember to do the MatLab assignment as well, which is on the syllabus. Just click the link and follow the instructions. Suggested problems: Sec. 3.2 # 2, 5, 6, 8, 12, 18, 22, 24, 25, 26 31; Sec. 3.3 # 2, 3, 5, 7, 11, 17, 21, 27; Sec. 3.4 # 1, 6, 9, 11, 14, 16, 26, 28, 30

Mandatory problems:

- (1) [8 pts] Use Abel's theorem to find the Wronskian for the differential equation $ty'' + 2ty' + te^t y = 0$ for t > 0.
- (2) Consider the IVP: y'' + 2y' + 6y = 0; y(0) = 2, $y'(0) = \alpha \ge 0$.
 - (a) [6 pts] Solve the IVP.
 - (b) [4 pts] Find α such that y = 0 when t = 1.
 - (c) [3 pts] Solve for t as a function of α and y. Then determine the smallest t for which y = 0. [Will need to use wolfram alpha/mathematica]
 - (d) [2 pts] Find $\lim_{\alpha \to \infty} t(\alpha, y = 0)$.
- (3) Consider the IVP 9y'' + 12y' + 4y = 0; y(0) = a > 0, y'(0) = -1.
 - (a) **[5 pts]** Solve the IVP.
 - (b) [2 pts] Find the critical value of a that separates solutions that become negative from those that are always positive.

Your homework raw score is: $\frac{n}{2m} \cdot M + \left(1 - \frac{n}{2m}\right) \cdot N = N + \frac{n}{2m}(M - N).$