

Suggested problems: Sec 5.1 # 18, 20, 21, 23; Sec 5.2 # 2(a,b), 4(a,b), 7(a,b); Sec 5.4 # 8, 17, 20; Sec 5.5 # 1, 2, 3, 12
Sec 6.1 # 3, 4, 6, 9, 13, 15, 21, 25, 26, 27 Sec 6.2 # 1, 2, 3, 7, 13, 24, 29, 30, 32, 33

*****Small Quiz on Friday, November, 11, 2016*****

Mandatory problems:

(1) Consider the ODE

$$(1-x)y'' + xy' - y = 0; x_0 = 0$$

(a) [10 pts] Use power series to solve the ODE and find the recurrence relation (i.e. solve for the a 's).

(b) [5 pts] Find the first four terms of your two linearly independent solutions.

(2) [5 pts each] Solve the following ODEs

(a) $x^2y'' + 4xy' + 2y = 0$

(b) $x^2y'' - 3xy' + 4y = 0$

(c) $x^2y'' + 3xy' + 5y = 0$

(3) [10 pts] Find all singular points and determine whether each is regular or irregular for the following ODE

$$x^2(1-x^2)y'' + \frac{2}{x}y' + 4y = 0$$

(4) [20 pts] Use Laplace transforms to solve the following IVP

$$y'' - 2y' + 2y = \cos t; y(0) = 1, y'(0) = 0.$$

Your homework raw score is: $\frac{n}{2m} \cdot M + \left(1 - \frac{n}{2m}\right) \cdot N = N + \frac{n}{2m}(M - N)$.