Math 4350-003 Rahman

Supplementary problems: Sec. 4.1 # 9b, 9c, 9d, 11a, 11b, 12b, 12c, 12d Do the previous supplementary problems if you haven't already. If you have, just rewrite them and I'll double count it.

Compulsory problems:

(1) [5 pts.] Prove that $\lim_{x\to 1} \sqrt{x} = 1$.

4.3.7) [7 pts.] Suppose $f(x) \leq g(x)$ for all x. Prove that if the limits exist

$$\lim_{x \to a} f(x) \le \lim_{x \to a} g(x). \tag{1}$$

4.2.10) [7 pts.] Give examples of functions f and g such that f and g do not have limits at a point c, but f + g and fg do.

4.2.9a) [11 pts.] Let $f, g: A \to \mathbb{R}$ and let c be a limit point of A. Prove that if $\lim_{x\to c} f(x)$ and $\lim_{x\to c} f(x) + g(x)$ exist, then so does $\lim_{x\to c} g(x)$.

Your homework raw score is: $\frac{n}{2m} \cdot M + \left(1 - \frac{n}{2m}\right) \cdot N = N + \frac{n}{2m}(M - N)$. For this homework, M = 30, m = 8, N is the number of compulsory problems you get correct, and n is the number of supplementary problems you complete. It should be noted that for the supplementary problems I will be looking for **full completion**, but I won't take off points for mistakes.